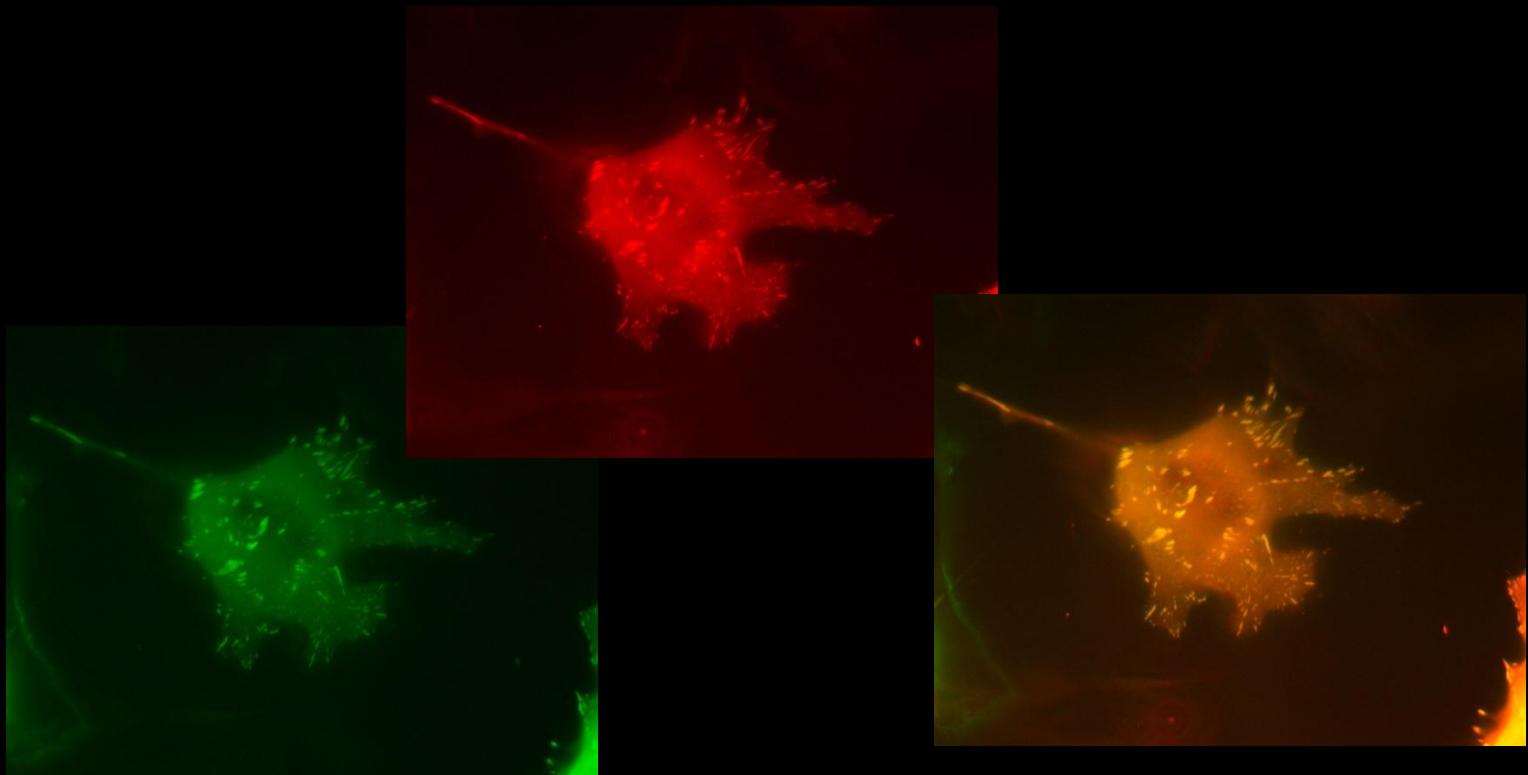


Fluorescence Spectroscopy III



Advanced fluorescence measurement

Fluorescence lifetime

Fluorescence lifetime is a complimentary measurement to spectral measurement. Most fluorophores has a signature lifetime as well as spectral. More important, some fluorophores have lifetimes that are more sensitive to environmental factors than their spectra.

The fluorescence decay of a fluorophore is governed by the following equation:

$$\frac{dN_e}{dt} = -(k + \Gamma)N_e$$

where N_e is the number of molecules in the excited state which is proportional to the fluorescence intensity. This differential equation can be easily solved:

$$F = F_0 e^{-(k+\Gamma)t} = F_0 e^{-t/\tau}$$

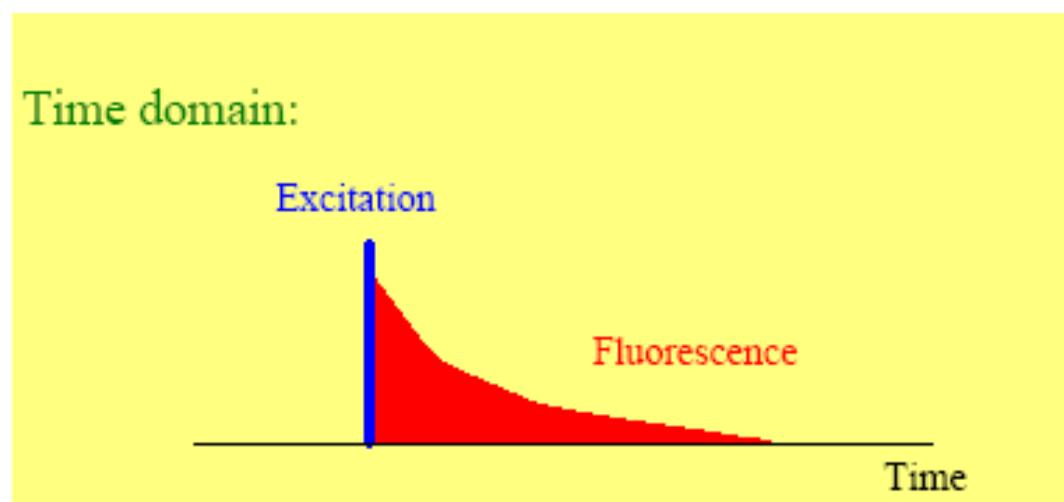
where F and F_0 are the instantaneous and initial fluorescence intensity. Therefore, we can see that fluorescence emission is a statistical process that is characterized by exponential decays. What if there are multiple decay pathways and multiple rates? In this case, the fluorescence decay will be multiple exponential:

$$\frac{dN_e}{dt} = -\left(\frac{1}{\tau_1} + \frac{1}{\tau_2} + \dots\right)N_e$$

$$F = F_0 e^{-\sum t/\tau}$$

As a matter of fact, fluorescence decay of most fluorophores in biological system often has multiple exponential decay that is characteristic both of the probe and its environment.

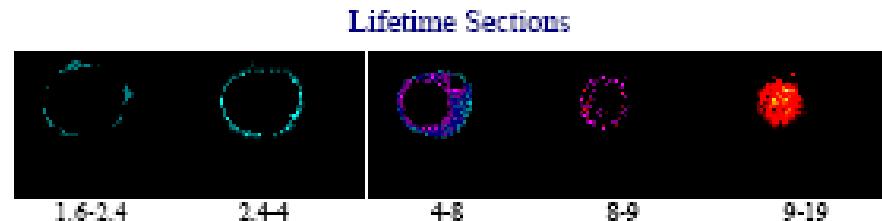
While fluorescence lifetime is a very useful parameter, it is however difficult to measure. As we have discussed before, fluorescence lifetime is typically on the time scale of nanoseconds. We therefore require very fast optics electronic to measure these events. Conceptually, the measurement can be done in the following way:



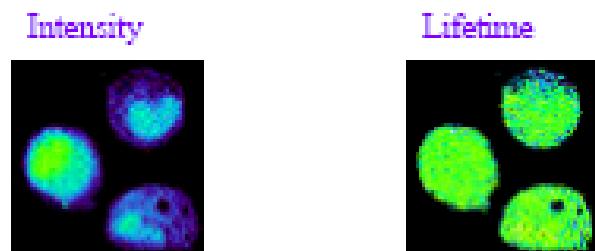
We will use a laser that can generate pulses that are very short compared with the fluorescence decay time (fs or ps). The fluorescence lifetime can then be measured by determining the time lapse between the excitation light and the first emission photon detected. One important catch to this scheme is that the photon detected for each excitation pulse has to be less than one.

Lifetime imaging and biological functions

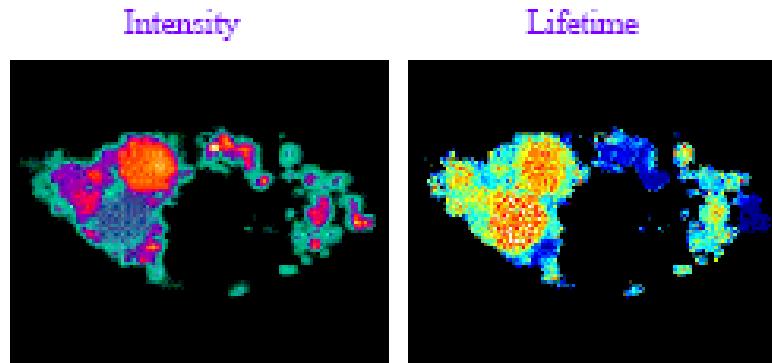
(1) Distinguish cellular organelles by multiple lifetime imaging



(2) Monitor metabolite concentration (Ca, pH etc)



(3) Monitor cellular processes such as proteolytic activity



Fluorescence Quenching

It is often very useful to measure the diffusion of small metabolites in a biological system; oxygen is a good example. As it turns out, a number of fluorophore, such as pyrene, with sufficiently long lifetime can be quenched by the presence of metabolite such as oxygen due to molecular collision. Upon collision, the fluorophore is de-excited non-radiatively.

The collision frequency is proportional to the concentration of the quencher and the rate equation in the presence of the quencher can be expressed as:

$$\frac{dN_e}{dt} = -(k_0[Q] + \Gamma)N_e$$

where $[Q]$ is the concentration of the quencher and k_0 is a proportionality constant related to the diffusivity of the reactants.

$$k_0 \propto (R_f + R_q)(D_f + D_q)$$

where R_f , R_q are the “collision” radii of the fluorophore and the quencher and D_f , D_q are the diffusion coefficients of the fluorophore and the quencher

Therefore, we have:

$$\tau^{-1} = k_0[Q] + \Gamma = k_0[Q] + \tau_0^{-1} = \tau_0^{-1}(1 + k_0\tau_0[Q])$$

Therefore, by measuring fluorescence lifetime, we can determine quencher concentration as long as the natural lifetime and the proportionality constant k can be calibrated.

The effect of quencher can also be studied by monitoring the steady state fluorescence emission. We will add a constant illumination term, I , to the fluorescence rate equation:

$$\frac{dN_e}{dt} = -(k_o[Q] + \Gamma)N_e + I$$

In the steady state, $\frac{dN_e}{dt} = 0$, and we have the fluorescence, F , signal:

$$(k_o[Q] + \Gamma)F = I$$

We can re-write this equation in the absence of quencher. The steady state fluorescence in the absence of quencher, F_0 , is:

$$\Gamma F_0 = I$$

Combining the last two equations, we get the Stern-Volmer equation:

$$\frac{F_0}{F} = 1 + k_o \tau_0 [Q]$$

For dynamic (collision) quenching process, the steady state fluorescence intensity is a linear function of quencher concentration.

The quenching process that we have described previously is called dynamic quenching where a fluorophore is de-excited by collision process in the excited state. For dynamic quenching, both the steady state fluorescence intensity and the fluorescence lifetime changes linearly with quencher concentration.

A molecule can also be quenched by a ground state process where the molecule is chemically bound to a quencher to form a “dark complex” – a reaction product that do not fluoresce. The ground state reaction can be described by the standard chemical kinetic rate equation where K_s is the association constant, $[F]$ is the concentration of the un-complexed fluorophores, $[F-Q]$ is the concentration of the complexes.

$$K_s = \frac{[F-Q]}{[F][Q]}$$

The total concentration of fluorophore, $[F]_0$, is given by:

$$[F]_0 = [F] + [F-Q]$$

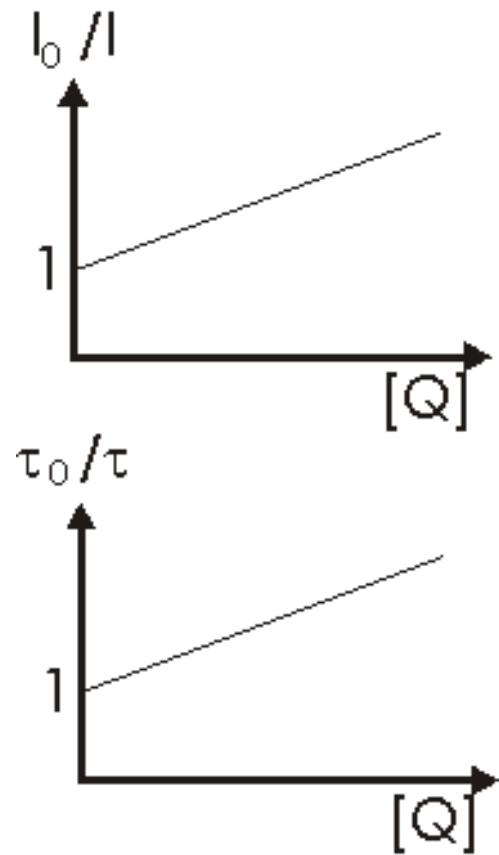
$$K_s = \frac{[F]_0 - [F]}{[F][Q]} = \frac{[F]_0}{[F][Q]} - \frac{1}{[Q]}$$

$$\frac{F_0}{F} = \frac{[F]_0}{[F]} = 1 + K_s[Q]$$

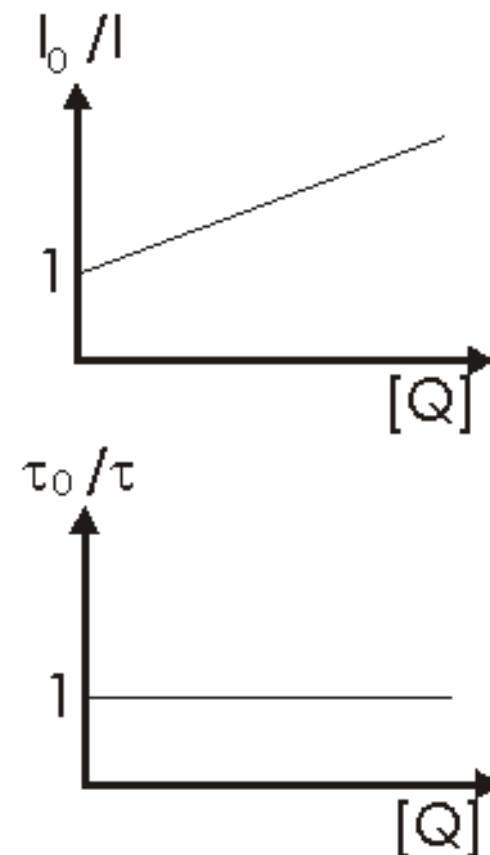
Therefore, in static quenching, the steady state fluorescence again decreases linearly with quencher concentration.

However, it is important to note that steady state quenching does NOT affect fluorescence lifetime as it does not affect the excited state and its effect is mainly the reduction of available fluorophores to be excited.

A summary of dynamic vs static quenching

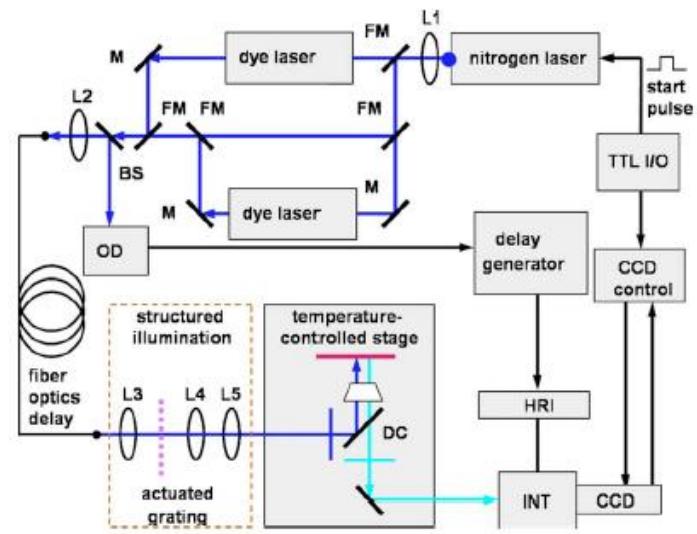
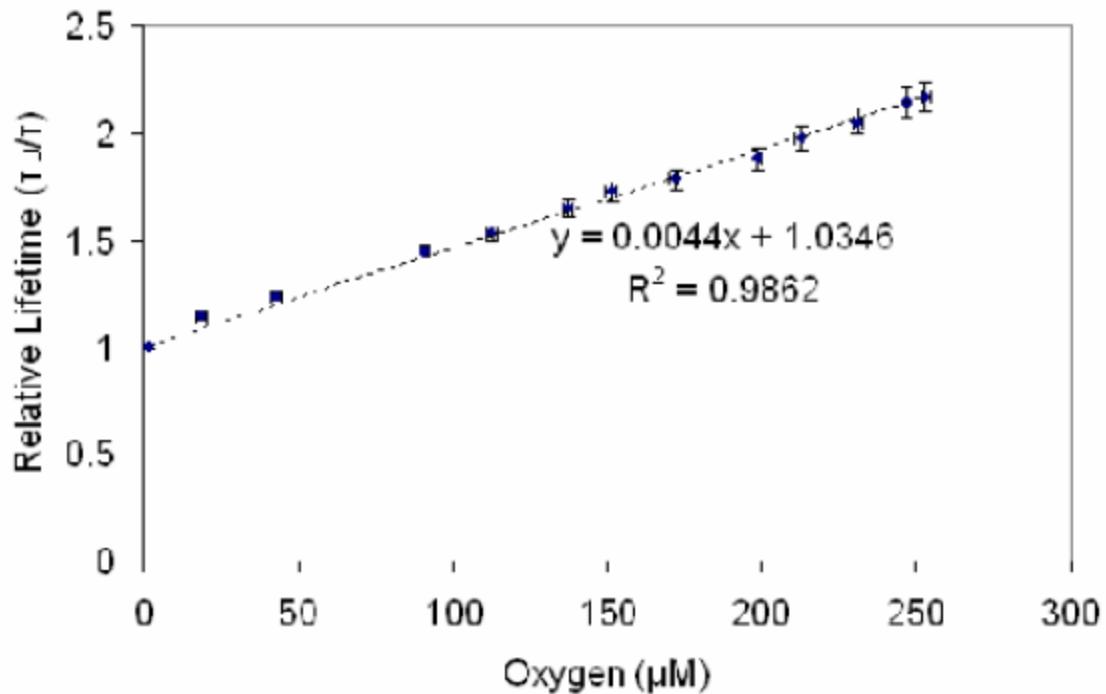


Dynamic
Quenching

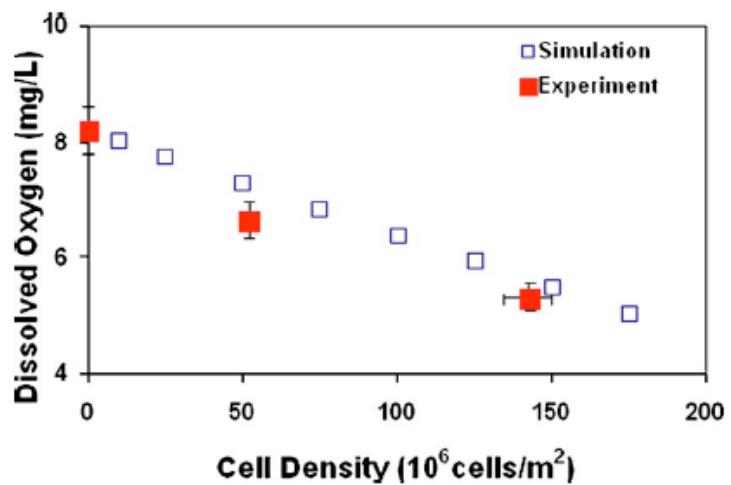
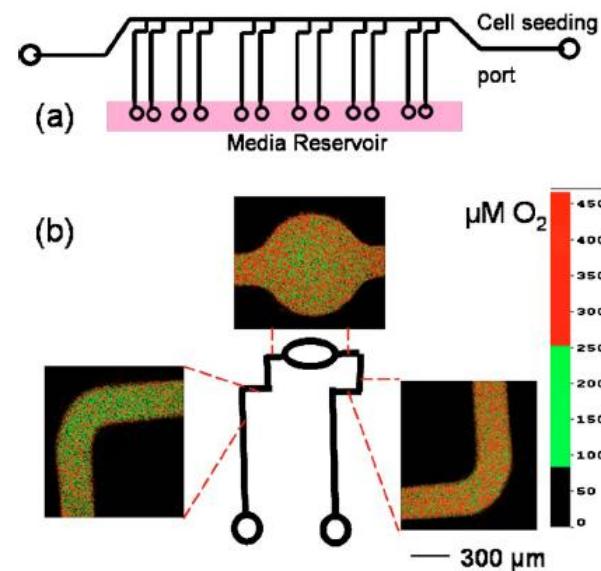
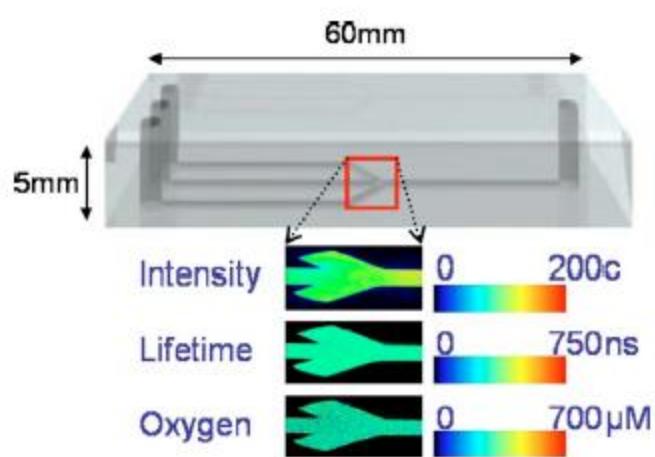


Static
Quenching

Imaging Oxygen Consumption in Microfluidic Devices



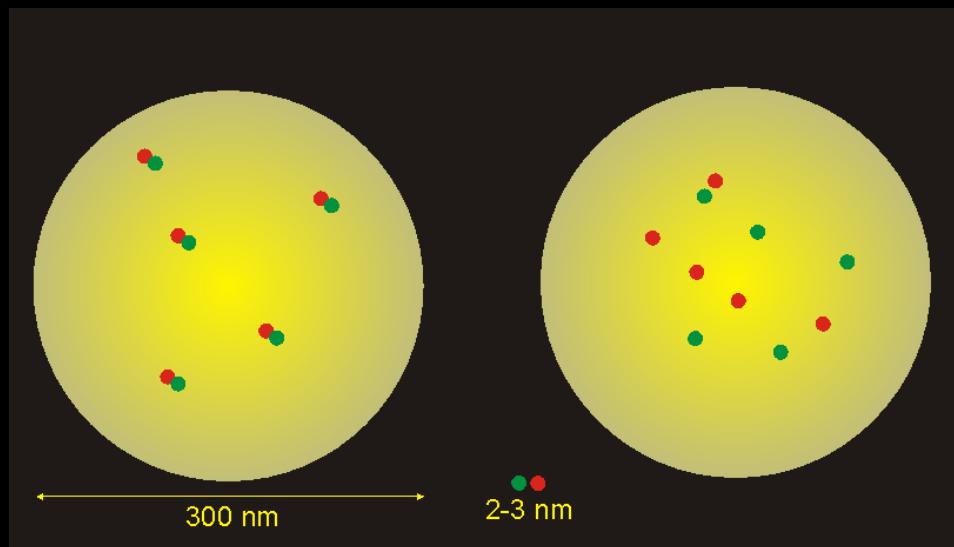
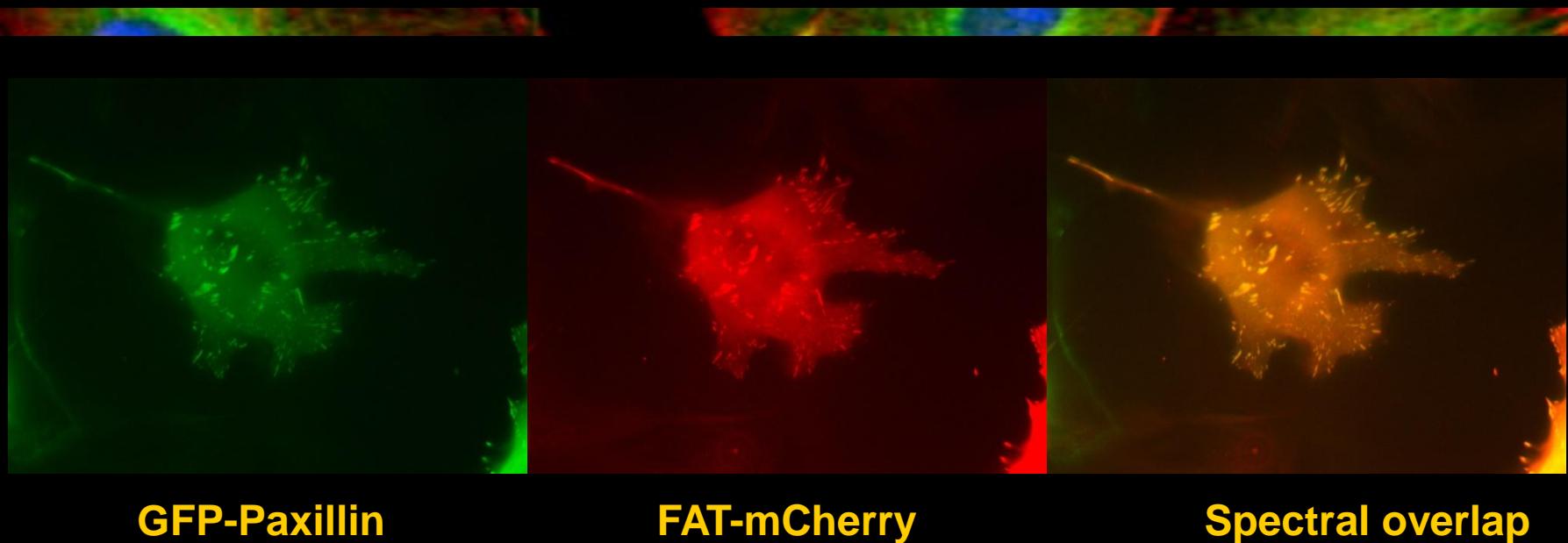
Imaging Oxygen Consumption in Microfluidic Devices



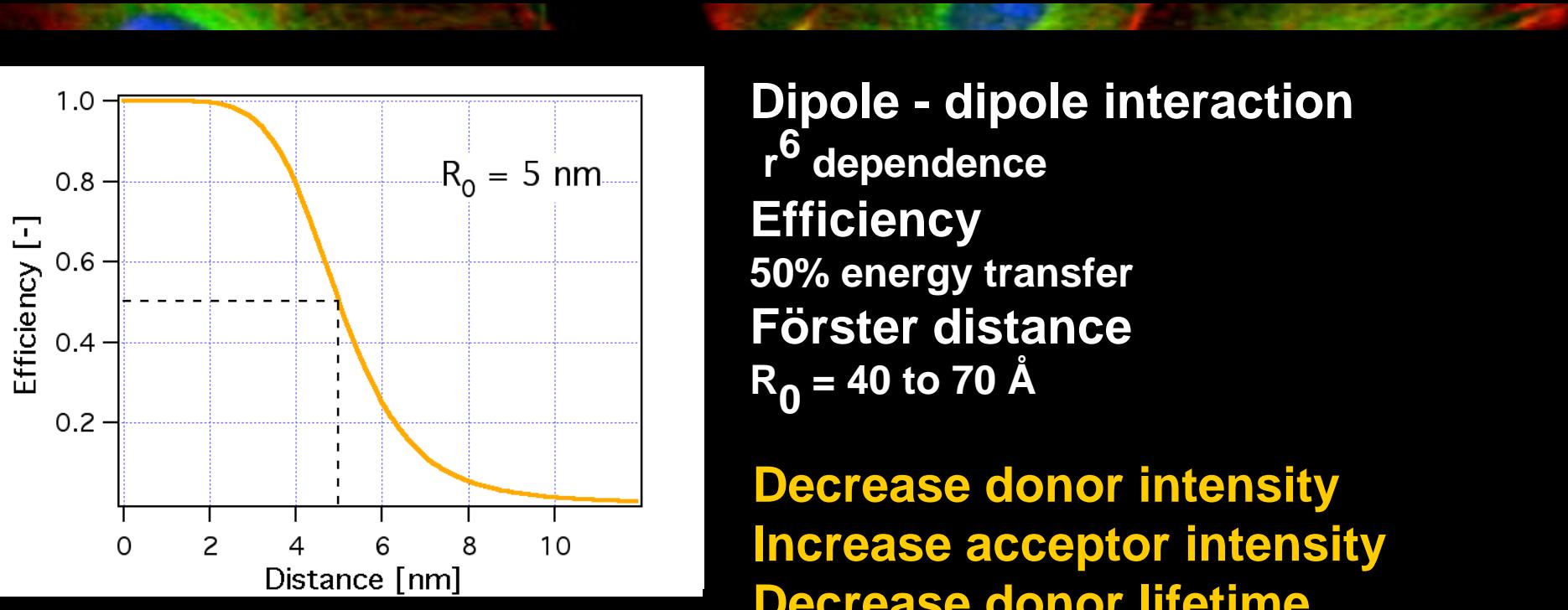
From Sud, OE 2006, Sub JBO Letters 2006

Paxillin-FAT in endothelial cells

PLIF



Fluorescence Resonance Energy Transfer (FRET)



$$E = \frac{R_0^6}{R_0^6 + r^6} = 1 - \frac{F_{DA}}{F_D}$$

$$E = \frac{R_0^6}{R_0^6 + r^6} = 1 - \frac{\tau_{DA}}{\tau_D}$$

$$R_0^6 = \frac{9000 \ln(10) \kappa^2 \phi_D}{128 \pi^5 N_A n^4} J$$

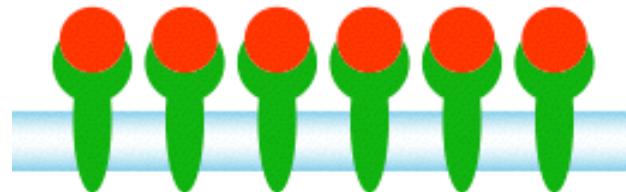
$$\text{where, } J = \frac{\int F_D(\lambda) \varepsilon_A(\lambda) \lambda^4 d\lambda}{\int F_D(\lambda)}$$

Bound counting

1. High receptor concentration,
No ligand



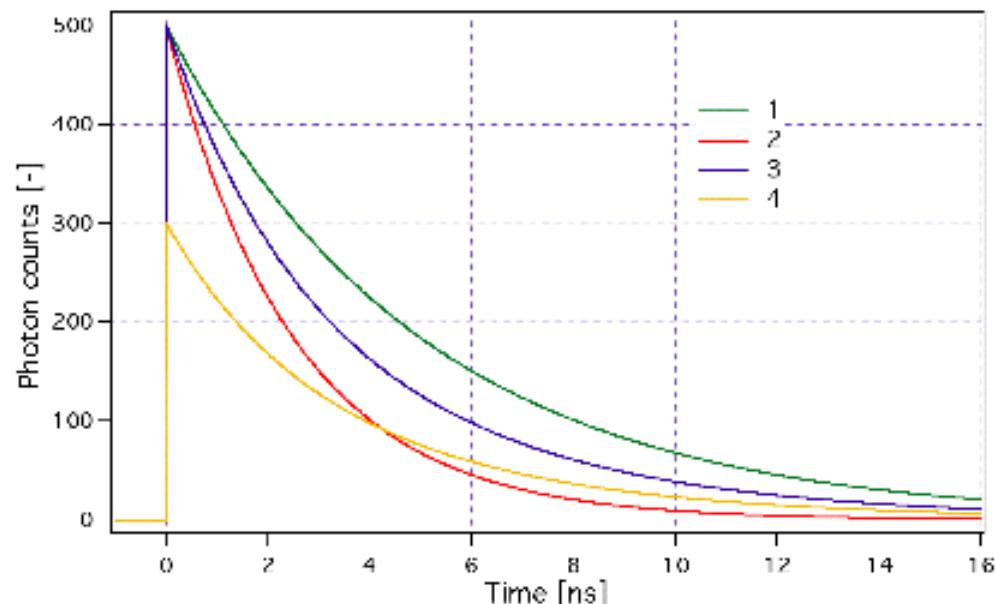
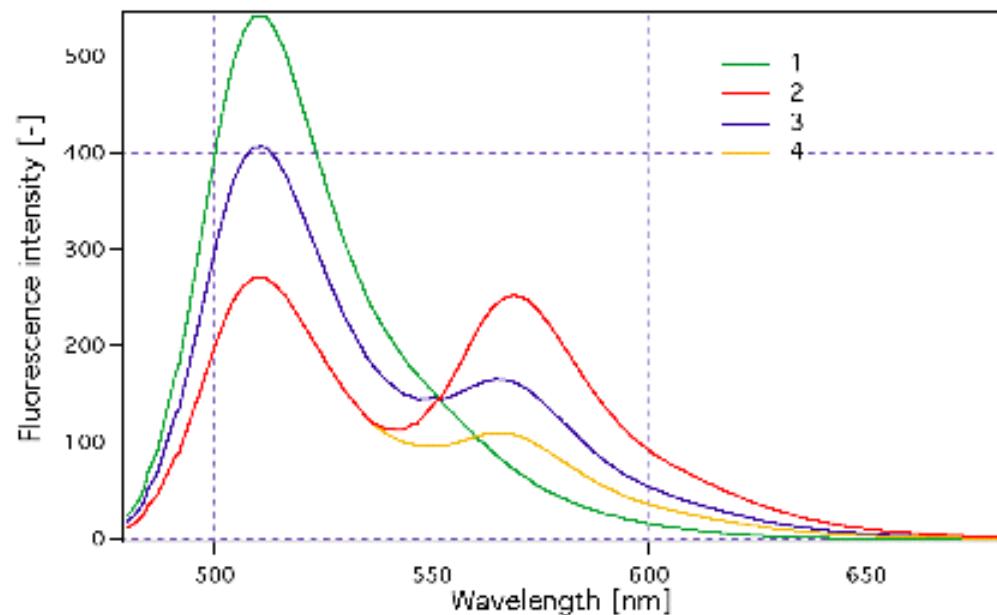
2. High receptor concentration,
Full ligand coverage



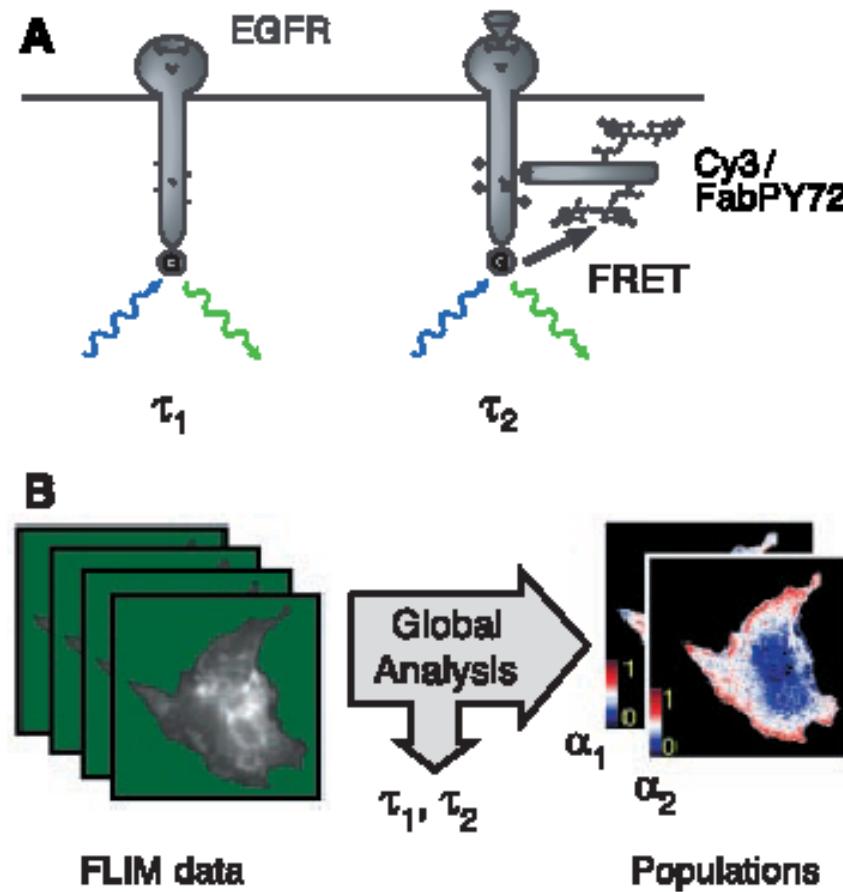
3. High receptor concentration,
low ligand coverage



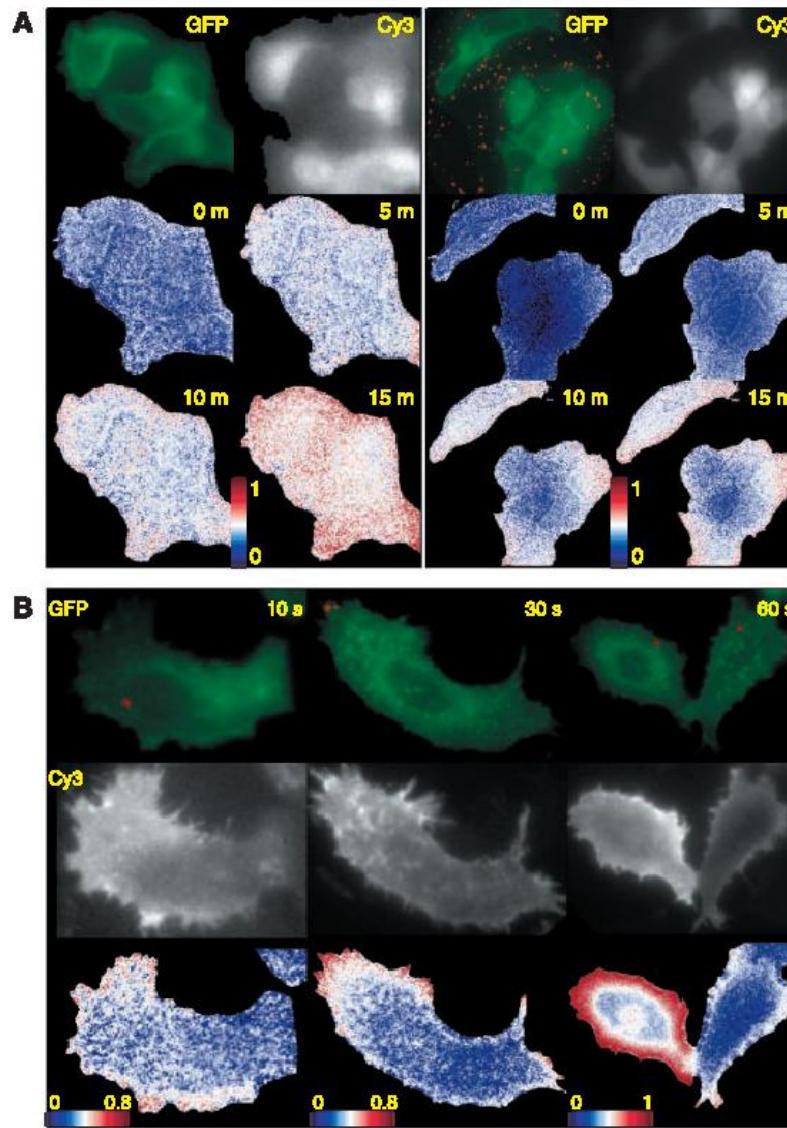
4. Low receptor concentration,
low ligand coverage



Apply Lifetime Resolved FRET to Study Receptor Mediated Signaling I



Apply Lifetime Resolved FRET to Study Receptor Mediated Signaling II



Verveer, Science 2000

Apply Lifetime Resolved FRET to Study Receptor Mediated Signaling III

