# Optimal Feed Rate for Maximum Ethanol Production

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#### **Outline**

- Chemostats and industrial ethanol manufacturing
- Saccharomyces cerevisiae and the fermentation process
- The role of glucose feed concentration in the fermentation process
- A mathematical model of EtOH production in a chemostat environment
- Maximization of EtOH production using free final time optimal control problem
- Optimal feed flow rate

### How Ethanol is produced on the industrial level

- Ethanol fermentation produces ethanol for use in food, beverages, and fuel.
- Yeast convert sugars, like glucose, into cellular energy.
- Ethanol and carbon dioxide are by products of this process.
- Fermentation occurs in large fermentation tanks.
- The enzyme alpha-amylase is added to tanks to break down corn starch into shorter carbohydrate chains called dextrins.
- During saccharification process the enzyme glucoamylase is added to mixture to break down dextrins into glucose.
- Starch is converted to simple sugars, yeast is added to convert glucose into ethanol and carbon dioxide.
  - https://www.osha.gov/dts/osta/otm/otm\_iv/descriptions.pdf

# Chemostats Can Be Used to Model Industrial Ethanol Production

- Chemostat cultures have been used by researchers as a tool to simulate the different stages of industrial ethanol production.
- Chemostat cultures allows scientists to gather data regarding metabolic processes of yeast cells.
- Enable researchers to test the effects of specific nutrients on ethanol production.

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# Saccharomyces cerevisiae is the Most Relevant Yeast Strain in Ethanol Production

- Saccharomyces cerevisiae is commonly used in winemaking, banking and brewing
- S. cerevisiae perform the most common type of fermentation
- Ethanol becomes toxic to yeast cells at high concentrations
- S. cerevisiae is a preffered yeast strain due to its high stress tolerance and its ability to efficiently use carbon and nitrogen resources
- Goal of industrial ethanol production is to produce maximum ethanol in shortest period of time
- Most ethanol is produced in later stages, i.e. at or near zero growth rates and stationary phase

### The Flexibility of Saccharomyces cerevisiae

- S. cerevisiae can rapidly switch between respiratory and fermentative sugar metabolism in response to changes in availability of oxygen and fermentable sugars
- S. cerevisiae can increase catabolic rates an start accumulating large amounts of ethanol upon this transfer
- Glucose starved yeast can adapt when introduced to high glucose concentrations within minutes
- Pathways responsible for fermentation process can suddenly catalyze sugar at very high rates, which is why *S. cerevisiae* is the most preferred yeast in industrial ethanol production (Van den Brink, et. al 2008).

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- Conclusion

#### The Role of Glucose in Ethanol Fermentation

- Yeast contain enzyme called zymase which catalyzes fermentation process
- Glucose zymase → Ethanol + Carbon Dioxide
- $C_6H_{12}O_6$  (aq)  $\rightarrow 2C_2H_5OH$  (aq) +  $2CO_2$ (g)
- Glycolysis breaks down glucose to form pyruvate.
- When oxygen is not present pyruvate undergoes fermentation.

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# A mathematical model of Ethanol Production in a Continuous Culture

$$\frac{dX}{dt} = \mu X - \frac{F}{V}X$$

$$\frac{dS}{dt} = -\frac{\mu}{Y}X + \frac{F}{V}(S_0 - S)$$

$$\frac{dP}{dt} = \pi X - \frac{F}{V}P$$

$$\frac{dV}{dt} = F$$

#### **Parameters and Constants in Model**

- X = Cell mass concentration
- S = Glucose concentration
- P = Ethanol concentration
- μ = Specific growth rate
- $\pi$  = Specific productivity
- F = Feed rate
- Notation used in Wang, et. al (1999)

#### **Parameters and Constants Continued**

$$\bullet \mu = \frac{\mu_0}{1 + \frac{P}{K_p}} * \frac{S}{K_s + S}$$

$$\bullet \pi = \frac{\pi_0}{1 + \frac{P}{K_p}} * \frac{S}{K_s + S}$$

$$\bullet \pi = \frac{\pi_0}{1 + \frac{P}{K_p}} * \frac{S}{K_s + S}$$

• Growth equations from Wang, et. al (2008).

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# **Brief Explanation of Dynamic Optimization**

$$\bullet \begin{cases} \dot{x} = f(x(t), u(t), t) \\ x(0) = x_0 \end{cases}$$

- Goal: maximize objective function
- $J(u) = \int_{t_0}^{t_f} F(x(t), u(t), t) dt + \lambda [x(t_1)]$
- State variable depends on control variable.
- Decision maker chooses control variable at any given time
- Final time  $t_f$  in this case is free
- Dynamic optimization means we aren't looking for a single steadystate solution, but for an optimal path amongst all feasible paths for the system.

## **Transversality Condition For Optimal Path**

- $\dot{x} = f(X(t), S(t), P(t), V(t), u(t), t)$
- The Hamiltonian:
- $H(t) = f(X(t), S(t), P(t), V(t), u(t), t) + \lambda(t)g(X(t), S(t), P(t), V(t), u(t), t)$
- $H(t_f) = 0$ , extending beyond  $t_f$  has no value because ethanol production has already been maximized
- $H(t_f)$  cannot be negative, in that case it would have been optimal to finish fermentation earlier
- State variables are the elevation of the road, control variable is the direction of the road at each point, and  $t_f$  is the length of the road.

# A Mathematical Model of Ethanol Production in a Continuous Culture

$$\frac{dX}{dt} = \mu X - \frac{F}{V}X$$

$$\frac{dS}{dt} = -\frac{\mu}{Y}X + \frac{F}{V}(S_0 - S)$$

$$\frac{dP}{dt} = \pi x - \frac{F}{V}P$$

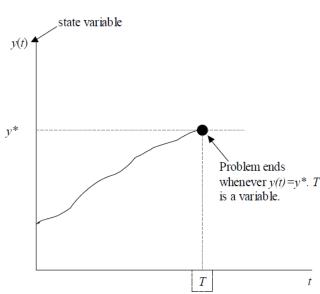
$$\frac{dV}{dt} = F$$

# **Optimal control of Fermentation Process**

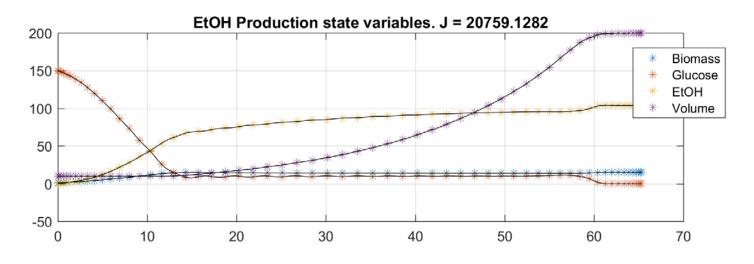
- Goal is to find optimal feeding rate, feed concentration, initial glucose concentration, and initial volume such that the ethanol production rate is maximized at the minimum fermentation time.
- The objective function is:

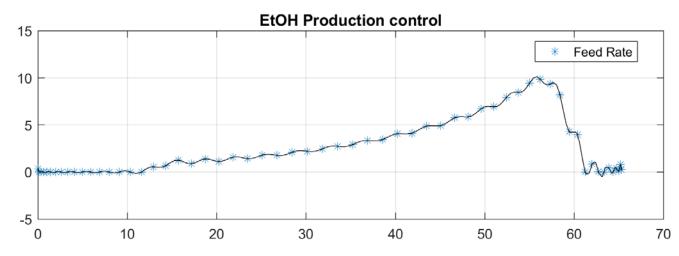
• 
$$\max_{F(t),S_0,S_f,V_0,t_f} J = P(t_f)V(t_f)$$

 My Matlab program used a direct collocation method to approximate numerical solutions for the optimal paths

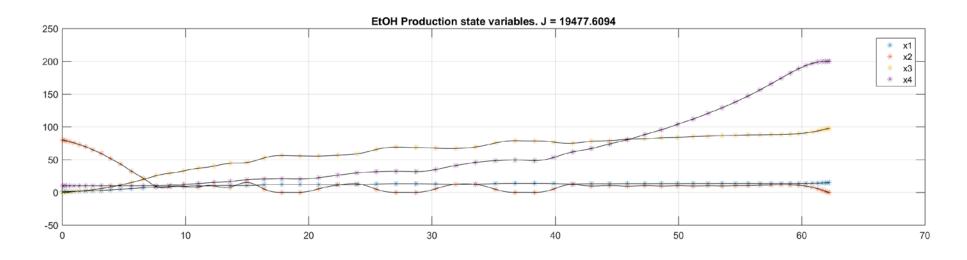


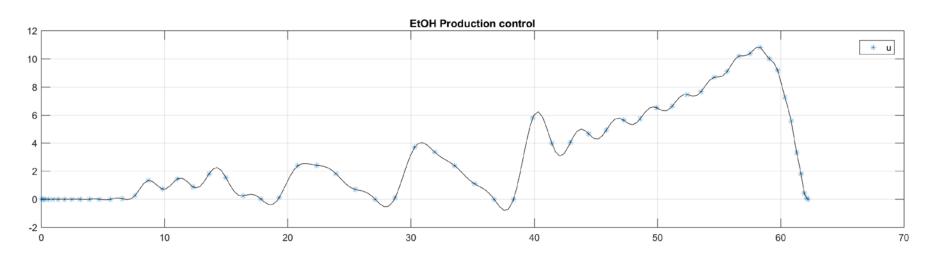
# **Optimal Paths For States and Control First Run**



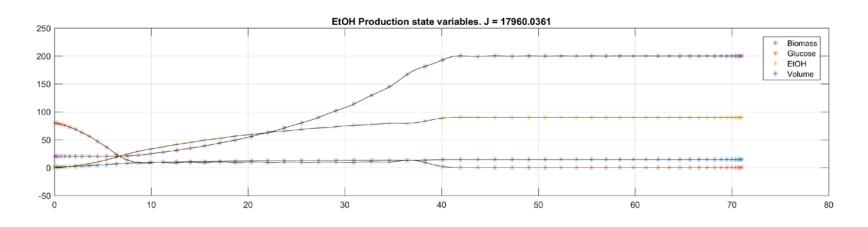


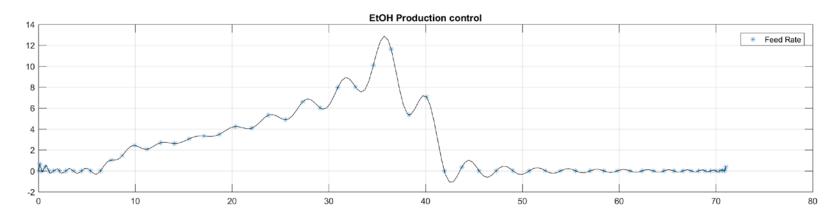
# Optimal Paths With 70 g/L Reduction In Initial Glucose





# **Optimal Paths With 10 L Increase in Initial Volume**





#### **Results From Previous Research**

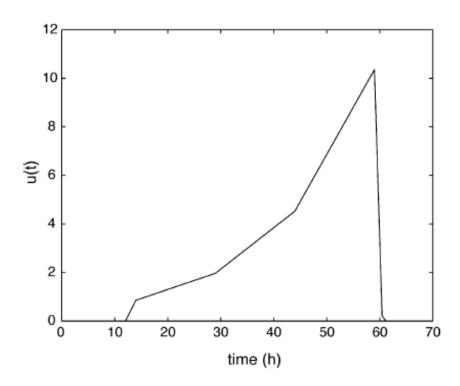


Fig. 7. Best optimal control ( $J=20839, t_{\rm f}=61.17\,{\rm h}$ ) for case study II.

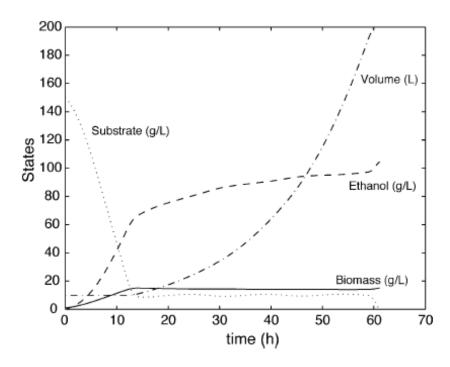


Fig. 8. State profiles for best optimal control, case study II.

### Values For Optimal Production Rate and Final Time

- Optimal final time for my first simulation was about 65 hours and the maximum ethanol production rate was 4.22kg/hr.
- Optimal final time for my second simulation was about 61 hours and maximum ethanol production rate was 3.96 kg/hr
- Values are similar to values obtained by previous researchers using a similar model but with higher number of collocation points.
- The feed rate concentration had an optimal path similar to the paths found in other research.
- Once EtOH concentration hits a critical point, biomass decreases sharply towards initial point, but EtOH continues to increase.
- This is consistent with (paper), which states that most EtOH is produced in the later stages of fermentation.

## **Response to Varying Constraints**

- Under the model I selected, maximum ethanol production is attained by adjusting feed rate concentration of glucose according to optimal path determined by solution to control problem.
- EtOH concentration increases despite decreases in biomass concentration of yeast.
- Feed rate and EtOH concentration are both constrained by total volume of chemostat/reactor.
- Reduction in initial glucose concentration by 70 g/l led to only a minor decrease in ethanol production rate.
- An increase in initial volume from 10 L to 20 L causes an increase in final time by > 10 hr

#### Conclusion

- It is possible to maximize EtOH production through optimal altering of feed rate over time.
- The optimal path of glucose feed rate is highly sensitive to changes in initial conditions.
- The maximum amount of ethanol production and maximum production rate are much less sensitive to changes in initial conditions.
- Maximum production is reach quickest when initial volume is low.

# **Acknowledgments**

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#### References

- Brauer, M. J., Saldanha, A. J., Dolinski, K., & Botstein, D. (2005). Homeostatic adjustment and metabolic remodeling in glucose-limited yeast cultures. *Molecular biology of the cell*, 16(5), 2503-2517.
- Van den Brink, J., Canelas, A. B., Van Gulik, W. M., Pronk, J. T., Heijnen, J. J., De Winde, J. H., & Daran-Lapujade, P. (2008). Dynamics of glycolytic regulation during adaptation of Saccharomyces cerevisiae to fermentative metabolism. *Applied and environmental microbiology*, 74(18), 5710-5723.
- Wang, F. S., & Cheng, W. M. (1999). Simultaneous Optimization of Feeding Rate and Operation Parameters for Fed-Batch Fermentation Processes. *Biotechnology Progress*, *15*(5), 949-952.
- Vázquez-Lima, F., Silva, P., Barreiro, A., Martínez-Moreno, R., Morales, P., Quirós, M., ... & Ferrer, P. (2014). Use of chemostat cultures mimicking different phases of wine fermentations as a tool for quantitative physiological analysis. *Microbial cell factories*, 13(1), 85.
- Gabriel, E., & Carrillo, U. (1999). *Optimal control of fermentation processes* (Doctoral dissertation, PhD Thesis, City University, London).
- Banga, J. R., Balsa-Canto, E., Moles, C. G., & Alonso, A. A. (2005). Dynamic optimization of bioprocesses: Efficient and robust numerical strategies. *Journal of Biotechnology*, 117(4), 407-419.